



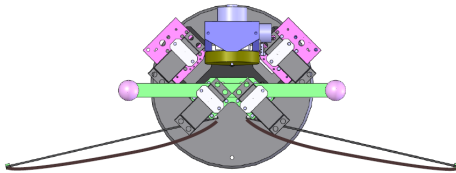
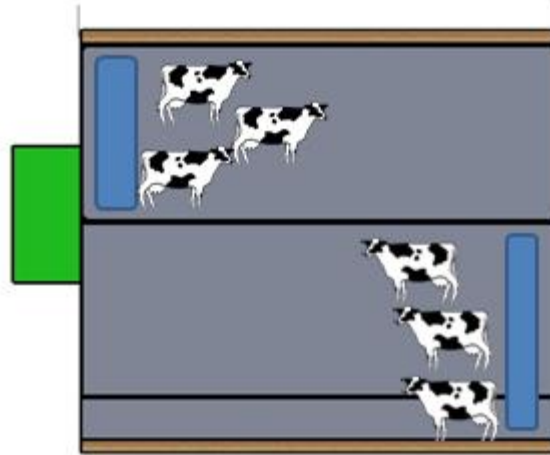
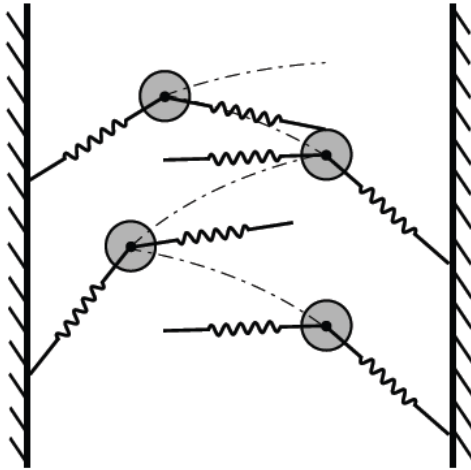
Technion
Israel Institute
of Technology

Amir Degani
Assistant Professor
Faculty of Civil and Environmental Engineering





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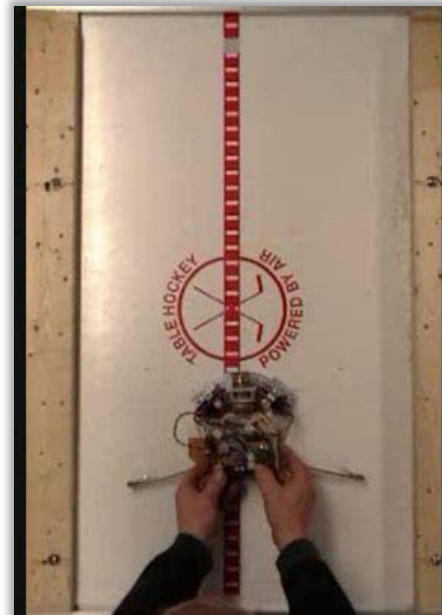
Dynamic Locomotion

Agriculture

Civil Applications



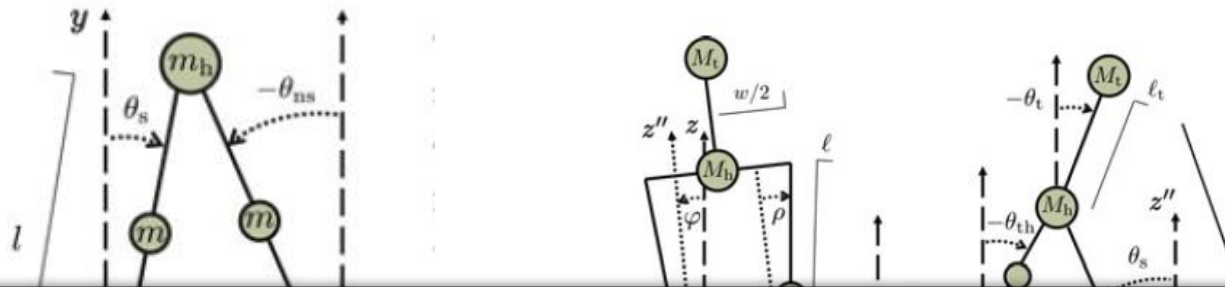
Dynamic Climbing



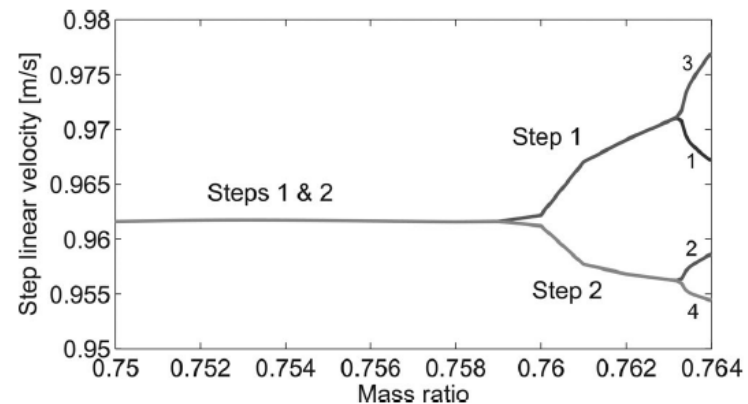
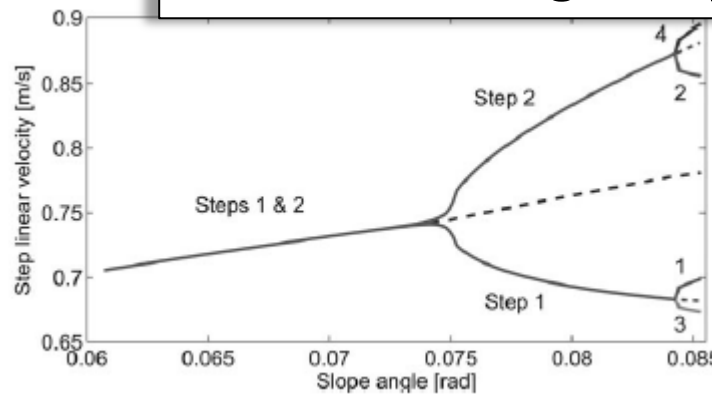
1mm

On the Mechanics of Functional Asymmetry in Bipedal Walking

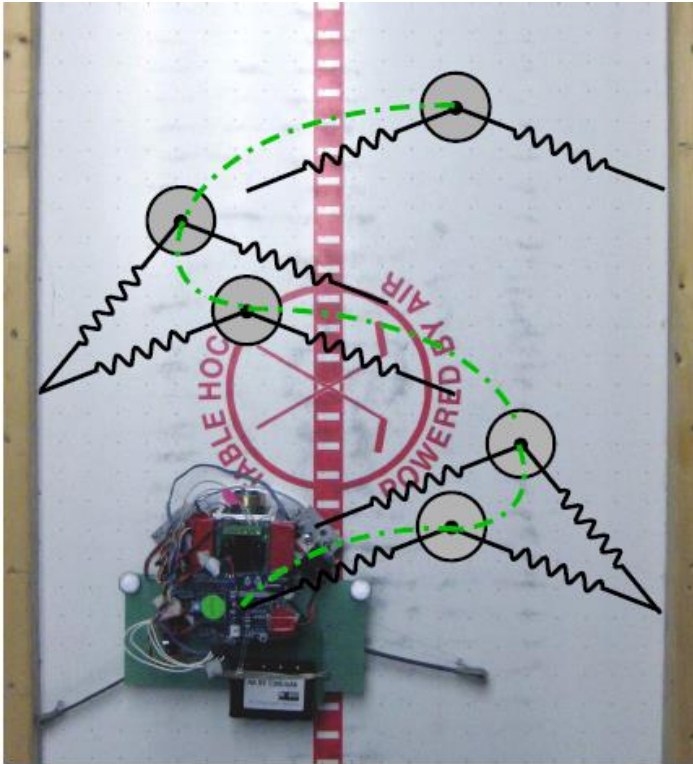
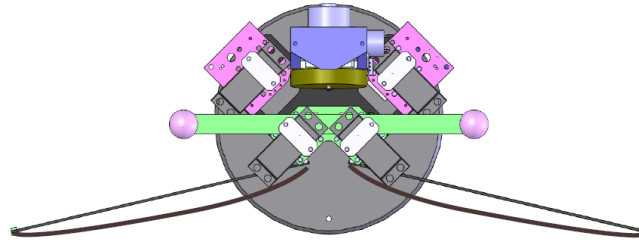
Robert D. Gregg*, *Member, IEEE*, Yasin Y. Dhaher, *Senior Member, IEEE*, Amir Degani, *Member, IEEE*,
and Kevin M. Lynch, *Fellow, IEEE*



Body mechanics, independent of neurophysiological mechanisms such as leg dominance, may contribute to able-bodied gait asymmetry.



The ParkourBot



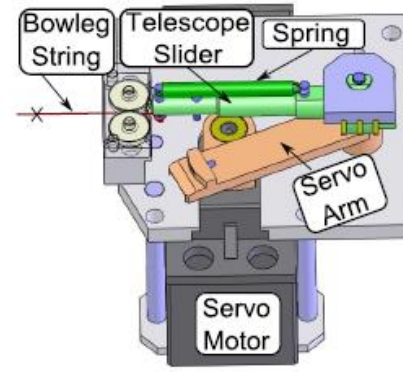
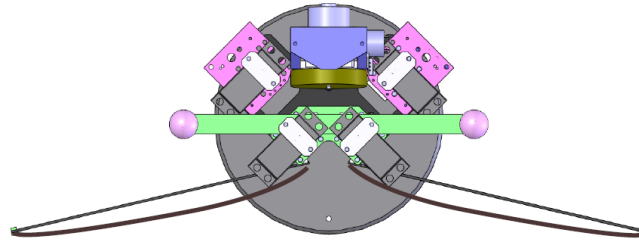
**Planar Bow Leg Hopper
Passive Stability Demonstration**

**H. Benjamin Brown, Jr.
Garth Zeglin**

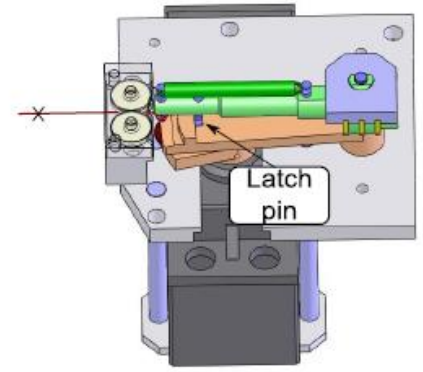
**Carnegie Mellon University
Robotics Institute**

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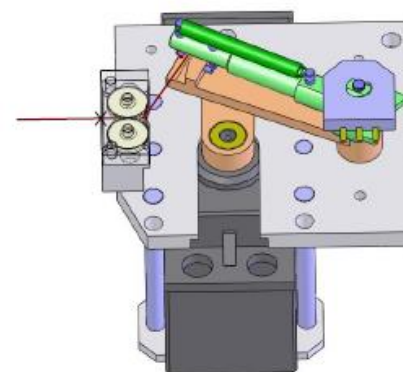
The ParkourBot



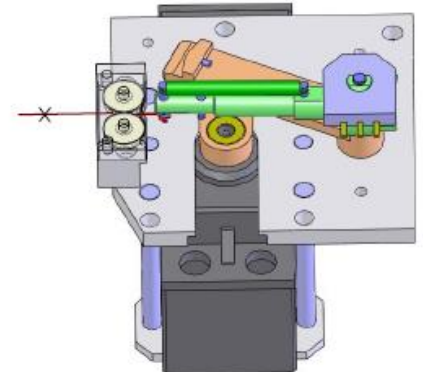
(a)



(b)



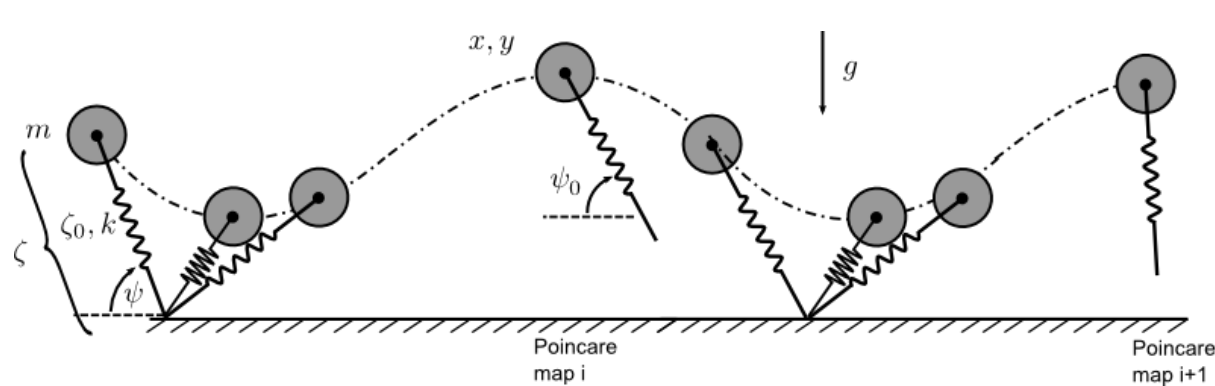
(c)



(d)

Horizontal Running Model

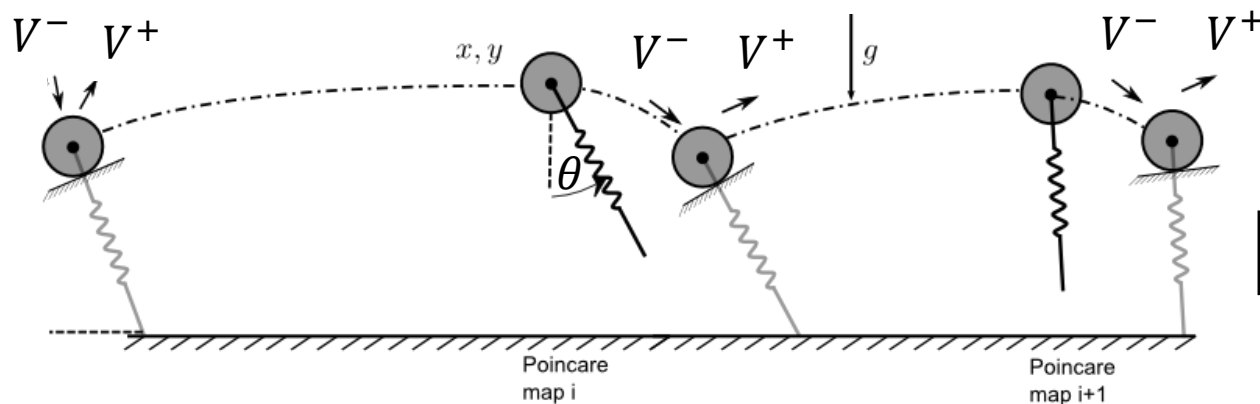
SLIP – Spring Loaded Inverted Pendulum



Stance:

$$\begin{bmatrix} \ddot{\zeta} \\ \ddot{\psi} \end{bmatrix} = \begin{bmatrix} -\frac{m}{k} (\zeta - \zeta_0 - g \cos(\psi) + \zeta \dot{\psi}^2) \\ -\frac{2\dot{\zeta}}{\zeta} \dot{\psi} - \frac{g}{\zeta} \sin(\psi) \end{bmatrix}$$

Horizontal "SPM" – Simplest Parkour Model*

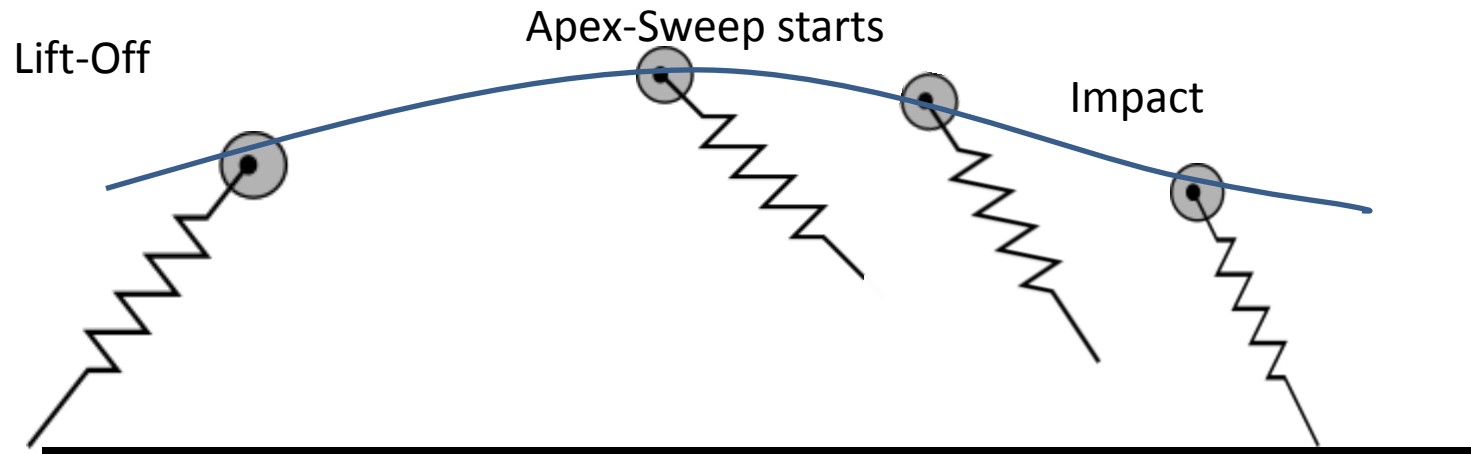


Impact:

$$\begin{bmatrix} V_x \\ V_y \end{bmatrix}^+ = \begin{bmatrix} V_x^- \cos(2\theta) + V_y^- \sin(2\theta) \\ V_x^- \sin(2\theta) - V_y^- \cos(2\theta) \end{bmatrix}$$

* Simplified model similar to: Zeglin, and Brown, 1998; Arslan and Sranli, 2012

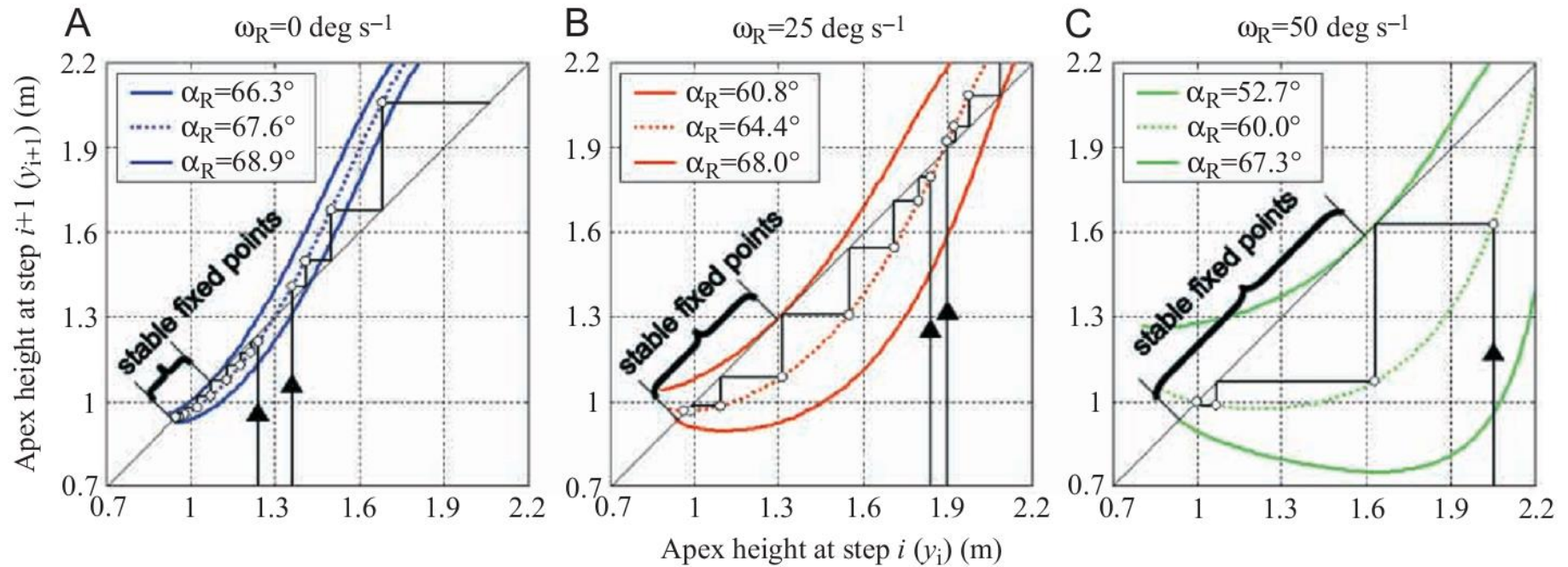
Swing-leg retraction



Taken from H. Geyer Website

Swing-leg retraction: a simple control model for stable running, Seyfarth, Geyer, and Herr; J. Exp. Biol. 2003

Swing-leg retraction

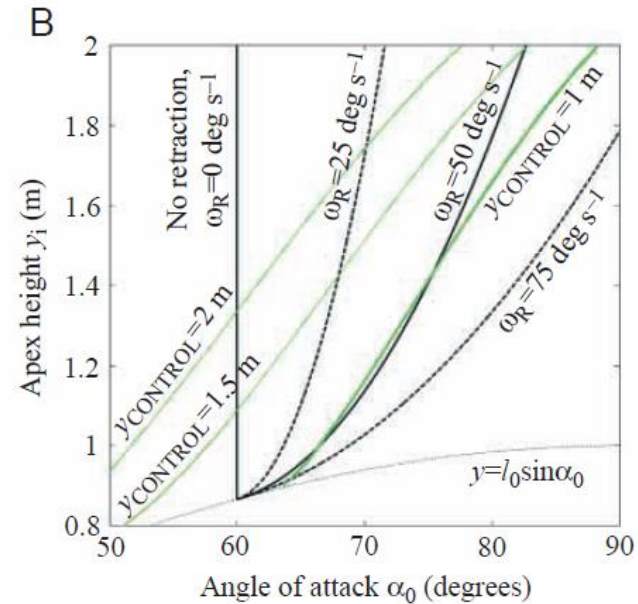
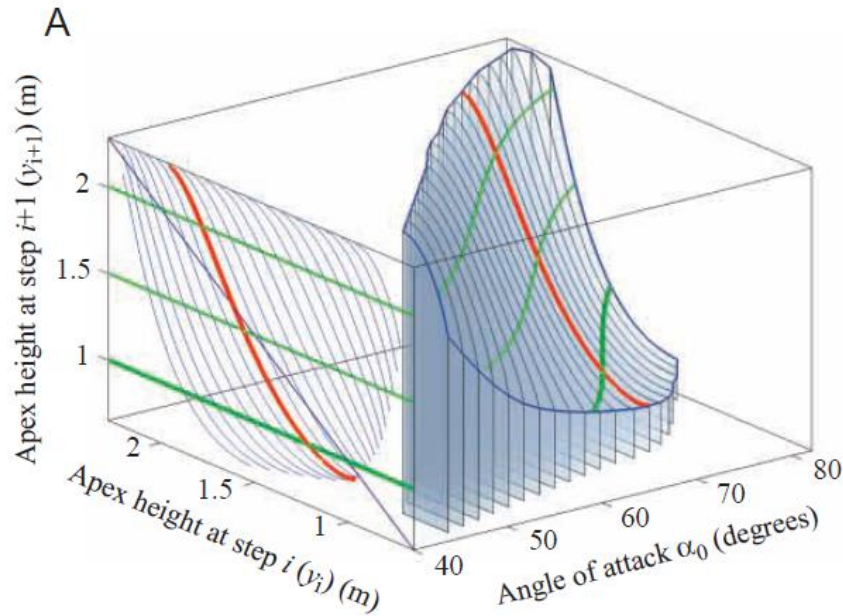


System Values:

$$m = 80 \text{ kg}; \zeta_0 = 1 \text{ m}; k = \frac{20 \text{ kN}}{m}; E = 1784 \text{ J}$$

Swing-leg retraction: a simple control model for stable running, Seyfarth, Geyer, and Herr; J. Exp. Biol. 2003

Sweep-Dead Beat Controller



System Parameters: $E = 1784 \text{ J}$, corresponds to $V_{x_0} = 5 \frac{\text{m}}{\text{s}}$, $m = 80 \text{ kg}$, $l_0 = 1 \text{ m}$, $K = \frac{20 \text{ kN}}{\text{m}}$

Green lines- Constant y_{i+1}

Red lines- $\alpha = 68^\circ$

Swing-leg retraction: a simple control model for stable running, Seyfarth, Geyer, and Herr; J. Exp. Biol. 2003

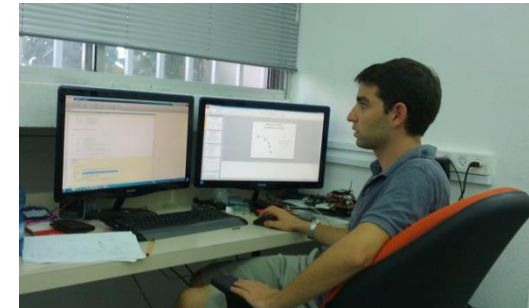
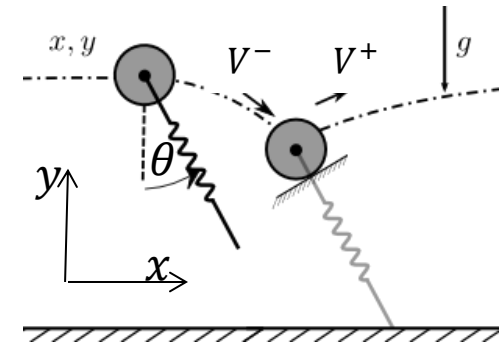
Horizontal "SPM"

- Closed form solution for stance phase:

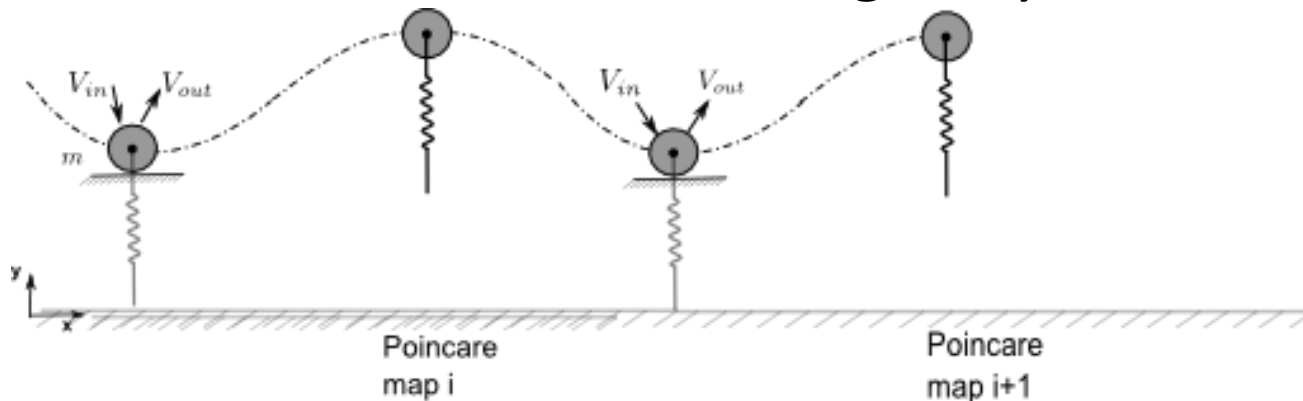
$$\begin{bmatrix} V_x \\ V_y \end{bmatrix}^+ = \begin{bmatrix} V_x^- \cos(2\theta) + V_y^- \sin(2\theta) \\ V_x^- \sin(2\theta) - V_y^- \cos(2\theta) \end{bmatrix}$$

- Fixed point is at $\theta = 0$

- Eigenvalue of the solution is 1 – Marginally stable



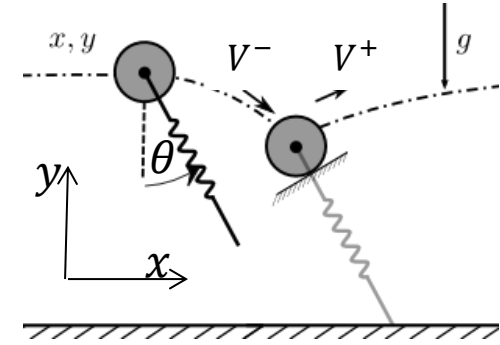
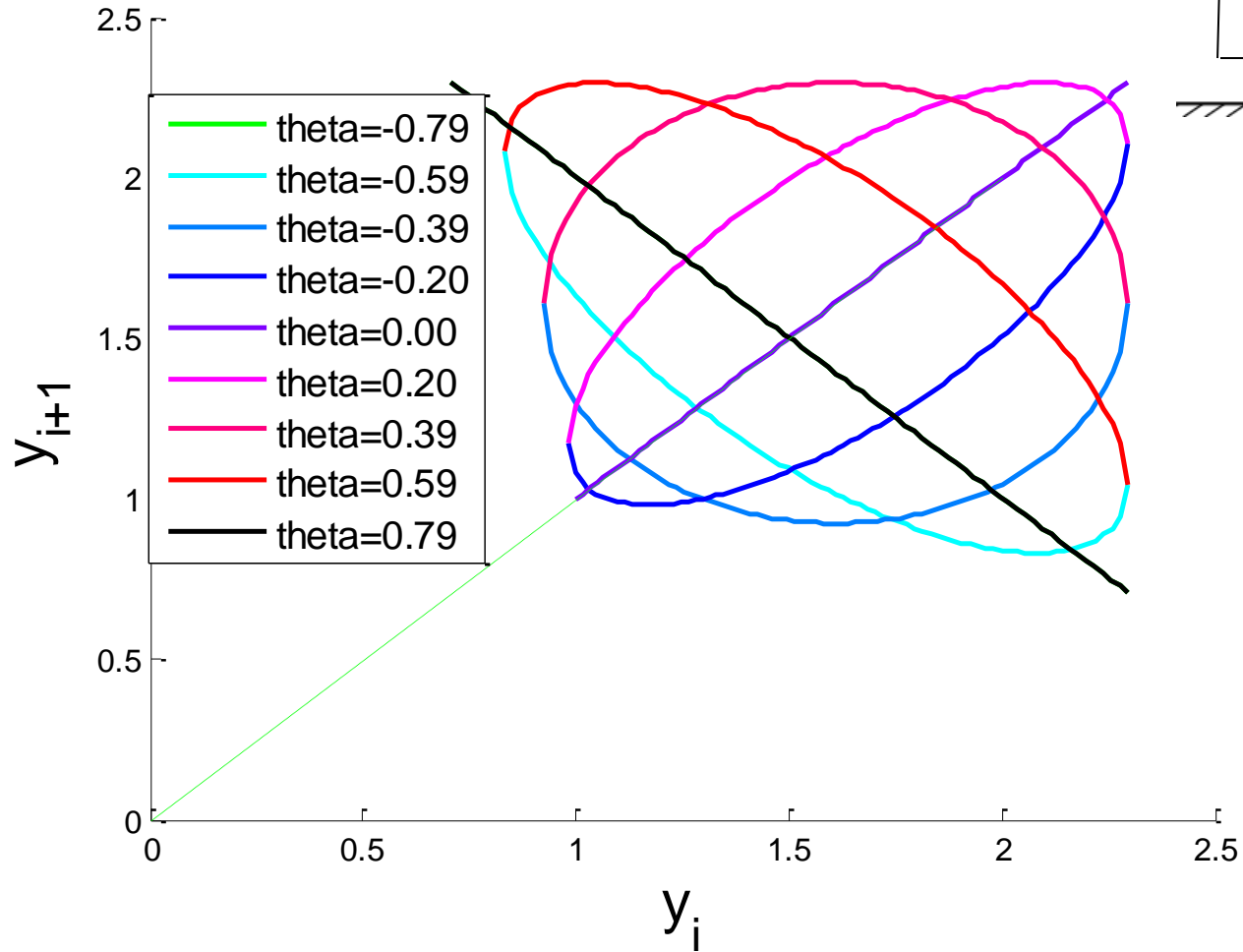
Naty Shemer – MSc Student



Horizontal "SPM" without sweep

$$\omega = 0$$

Apex Return map



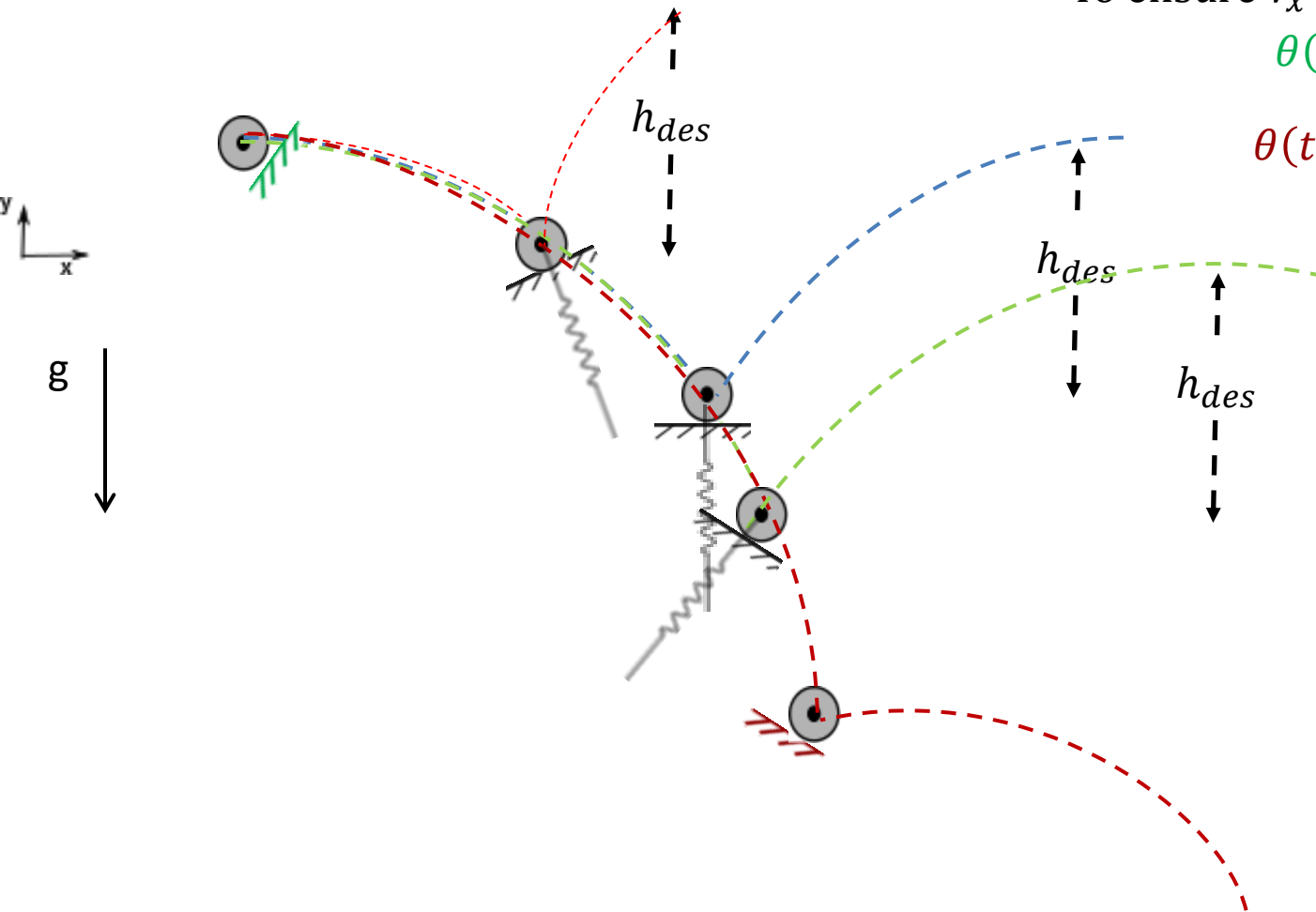
Horizontal “SPM” Dead-Beat Controller

Finding impact angle bounds:

To ensure $V_x^+ > 0$ & $V_y^+ < 0$

$$\theta(t = 0) < \frac{\pi}{4}$$

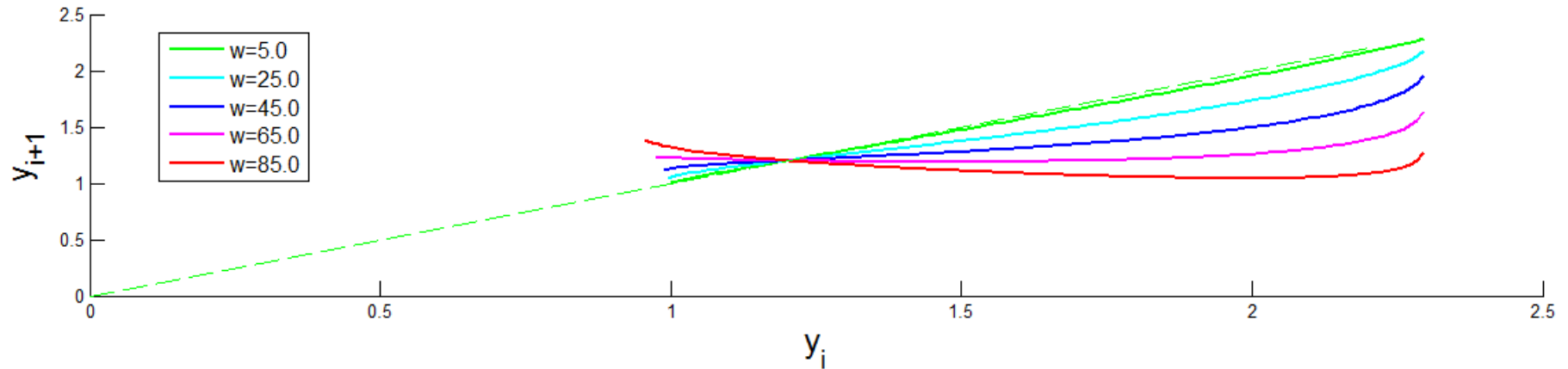
$$\theta(t = \infty) > \frac{3\pi}{4}$$



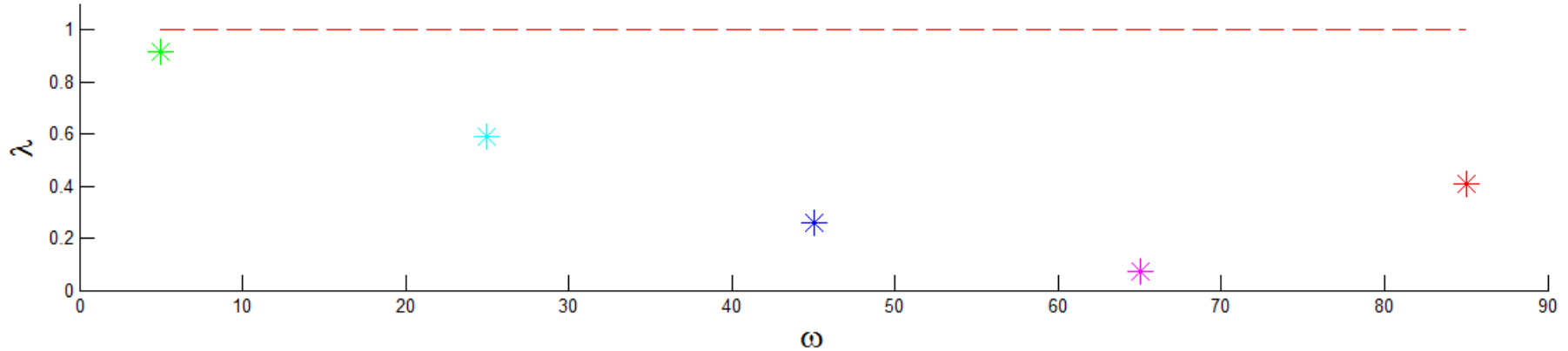
Horizontal "SPM" with Swing-Leg

$$\omega \neq 0$$

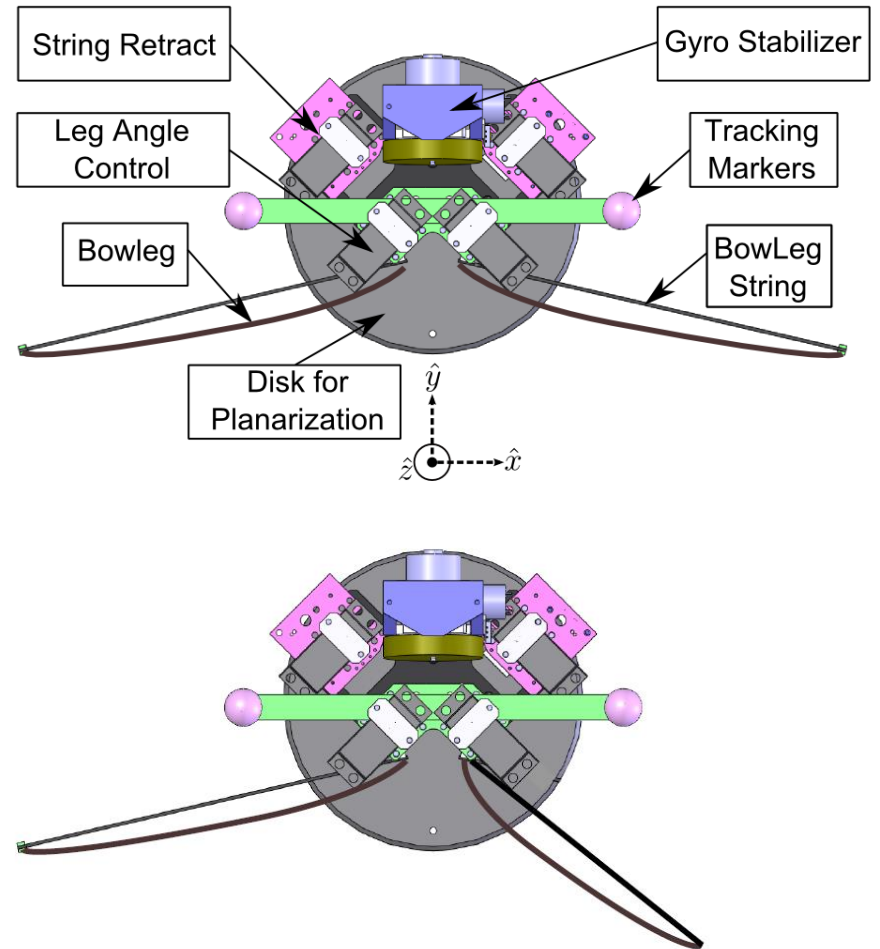
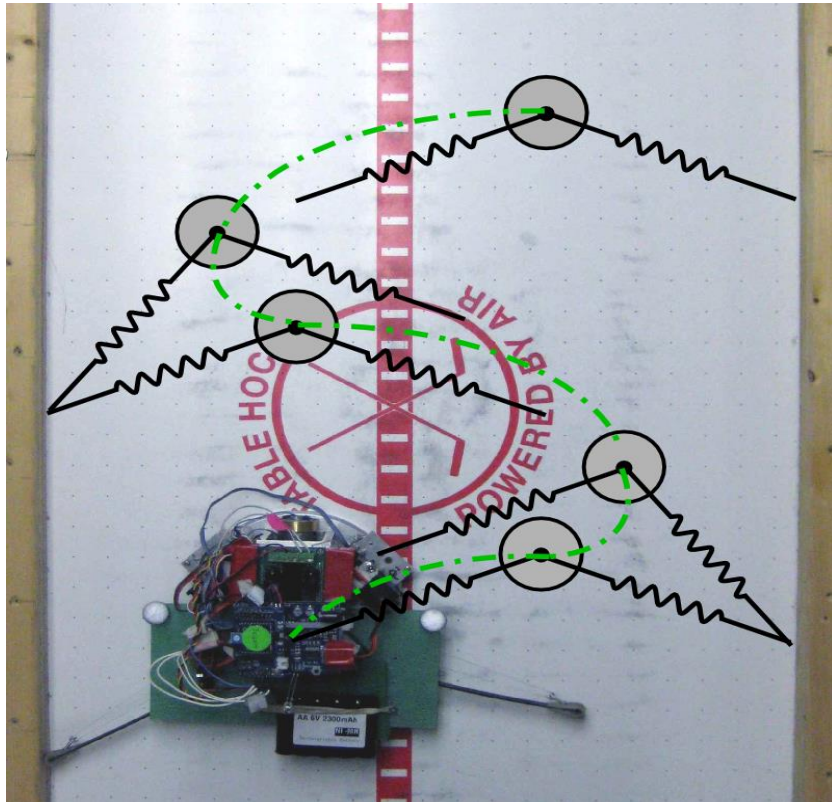
Apex Return map $h_{\text{des}} = 1.2$



stability eigenvalues $h_{\text{des}} = 1.2$



The ParkourBot

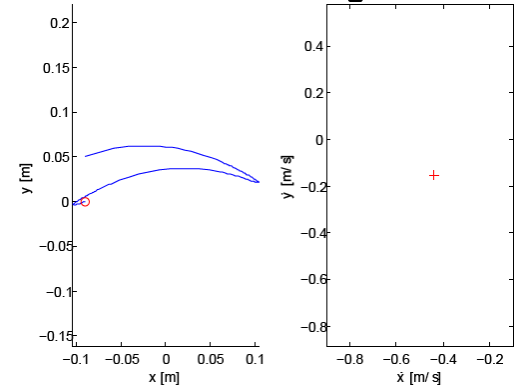


With Howie Choset, Matt Mason, Ben Brown (CMU) and Kevin Lynch (NU)

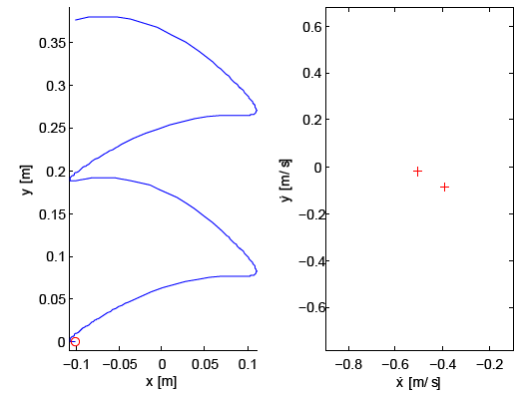
ParkourBot – Previous open loop



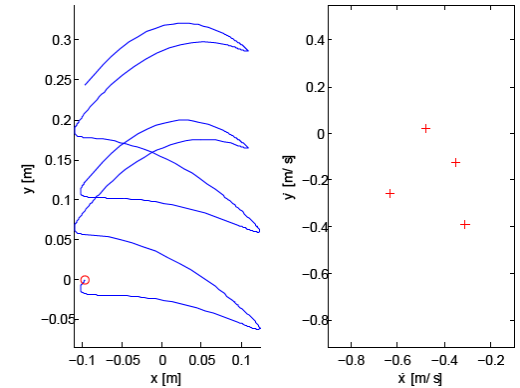
Period-1



Period-2



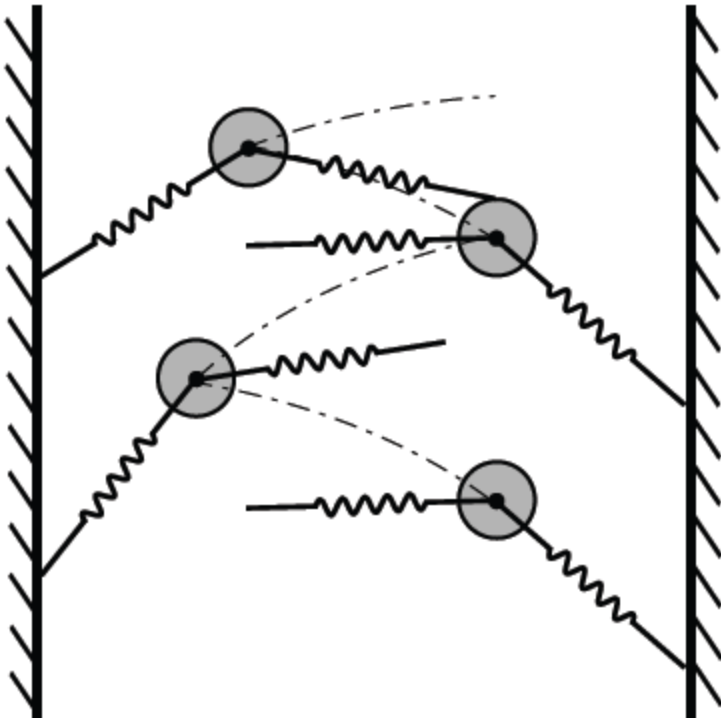
Period-4



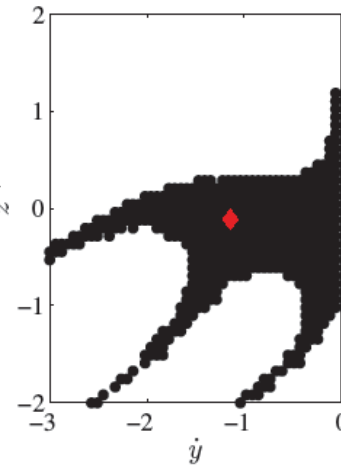
ParkourBot – Previous open loop

Vertical Movement Complications:

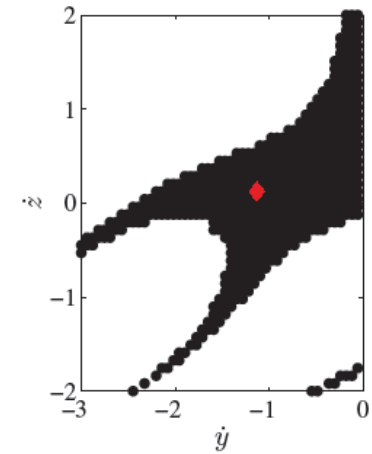
1. Apex doesn't always happen
2. Movement on the same axis as gravity
3. Poincare map is 2D



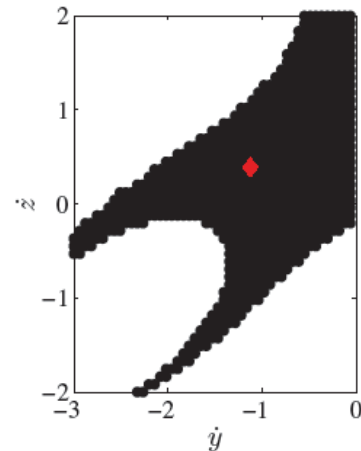
(a) Maximum eigenvalue vs. energy input.



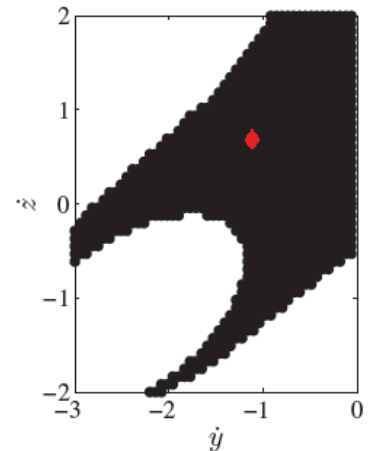
(b) $\zeta_0 = 0.8$



(c) $\zeta_0 = 0.75$



(d) $\zeta_0 = 0.7$



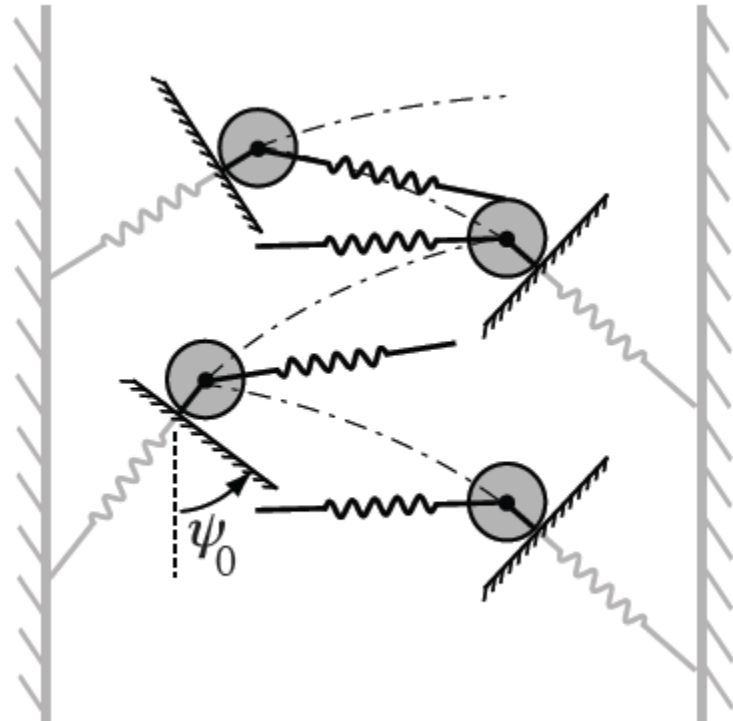
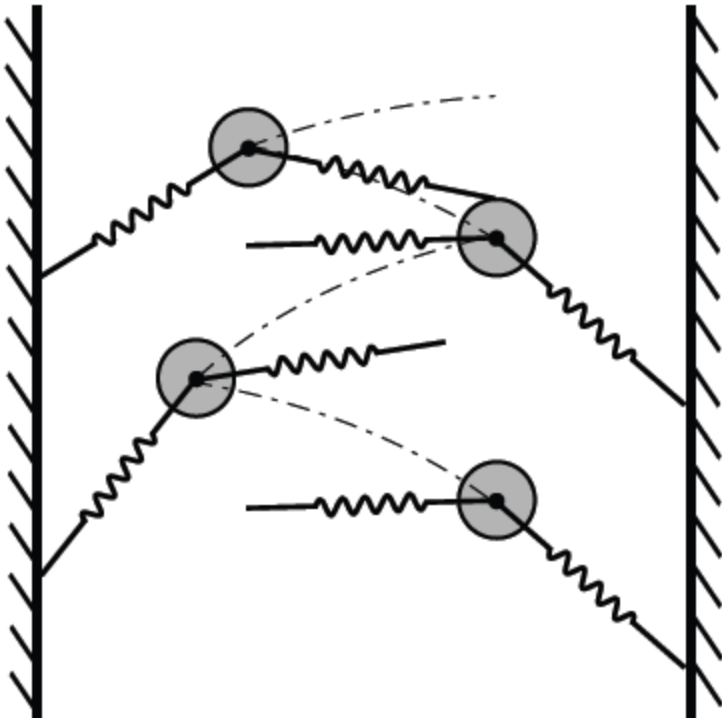
(e) $\zeta_0 = 0.65$

Vertical SPM

$$\ddot{\zeta} = k - k\zeta + \zeta\dot{\psi}^2 - \sin\psi - c_\zeta\dot{\zeta}$$

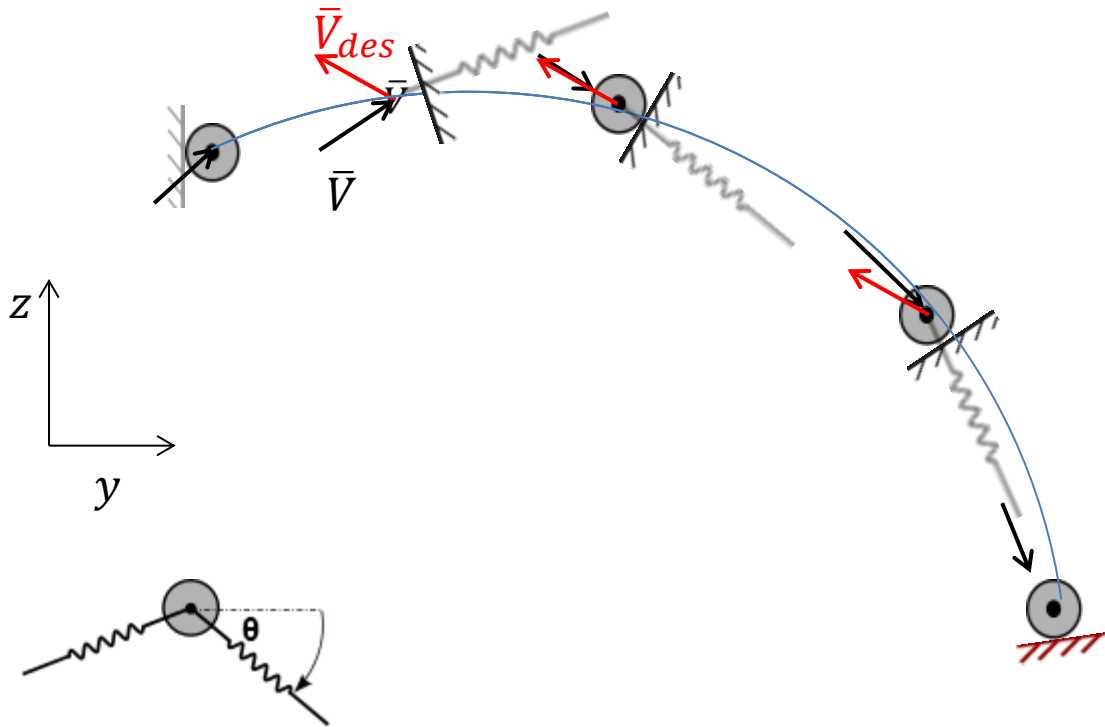
$$\ddot{\psi} = -\frac{1}{\zeta}(\cos(\psi) - 2\dot{\zeta}\dot{\psi}) - c_\psi\dot{\psi}$$

$$\begin{bmatrix} V_y \\ V_z \end{bmatrix}^+ = \begin{bmatrix} V_z^- \sin(2\theta) - V_y^- \cos(2\theta) \\ V_y^- \sin(2\theta) + V_z^- \cos(2\theta) \end{bmatrix}$$



Steady State Solution

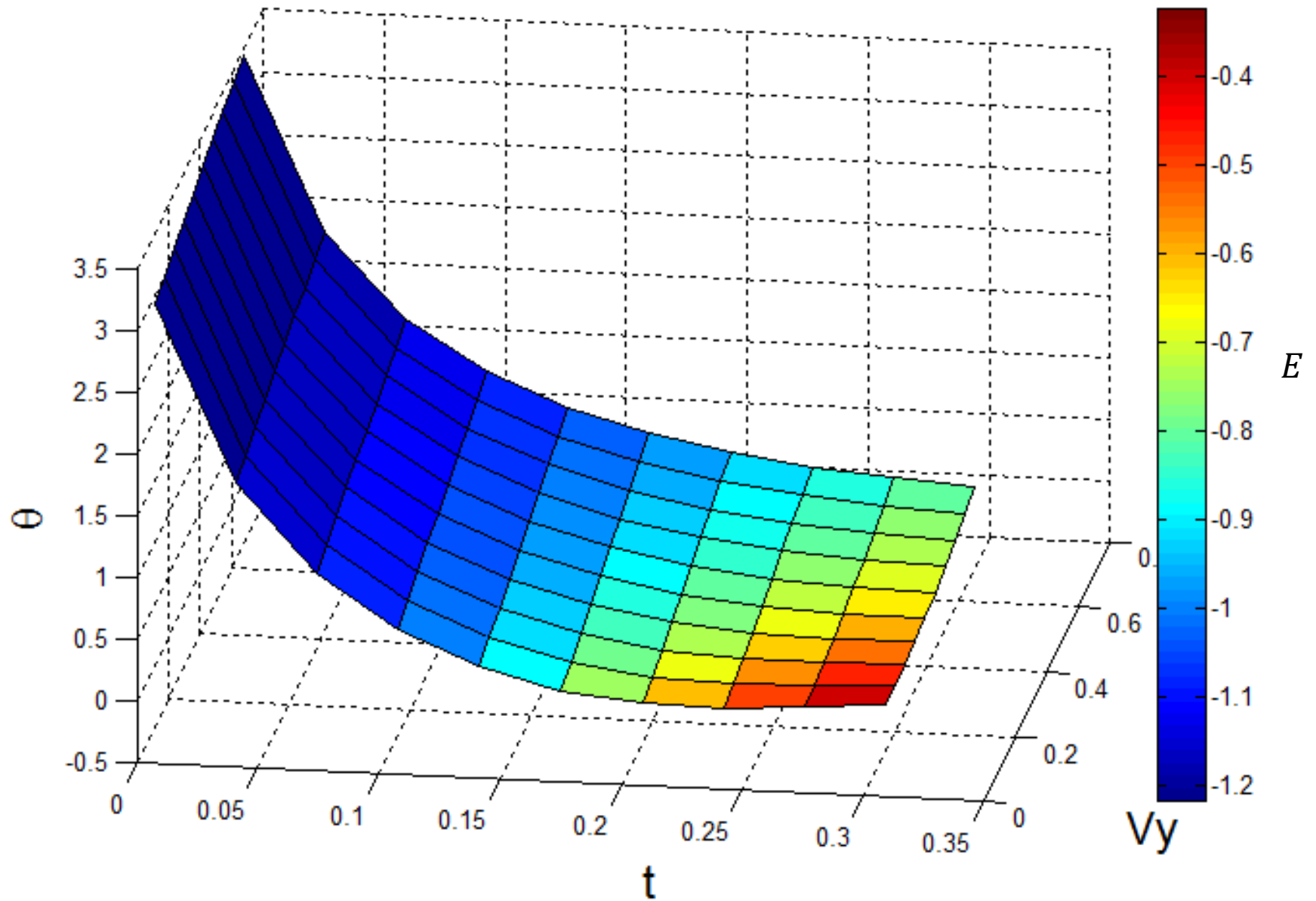
$$\begin{bmatrix} V_y \\ V_z \end{bmatrix}^+ = \begin{bmatrix} V_z^- \sin(2\theta) - V_y^- \cos(2\theta) \\ V_y^- \sin(2\theta) + V_z^- \cos(2\theta) \end{bmatrix}$$



In order to ensure
 $V_y^+ < 0$;

$$\theta(t = \infty) > 0$$

Dead-Beat control for $V_y = -0.34 V_z = 0.45$



Model Values: $V_{z0} = 0.45; g = 1.47; \epsilon = 0.7$

Non-Dimension

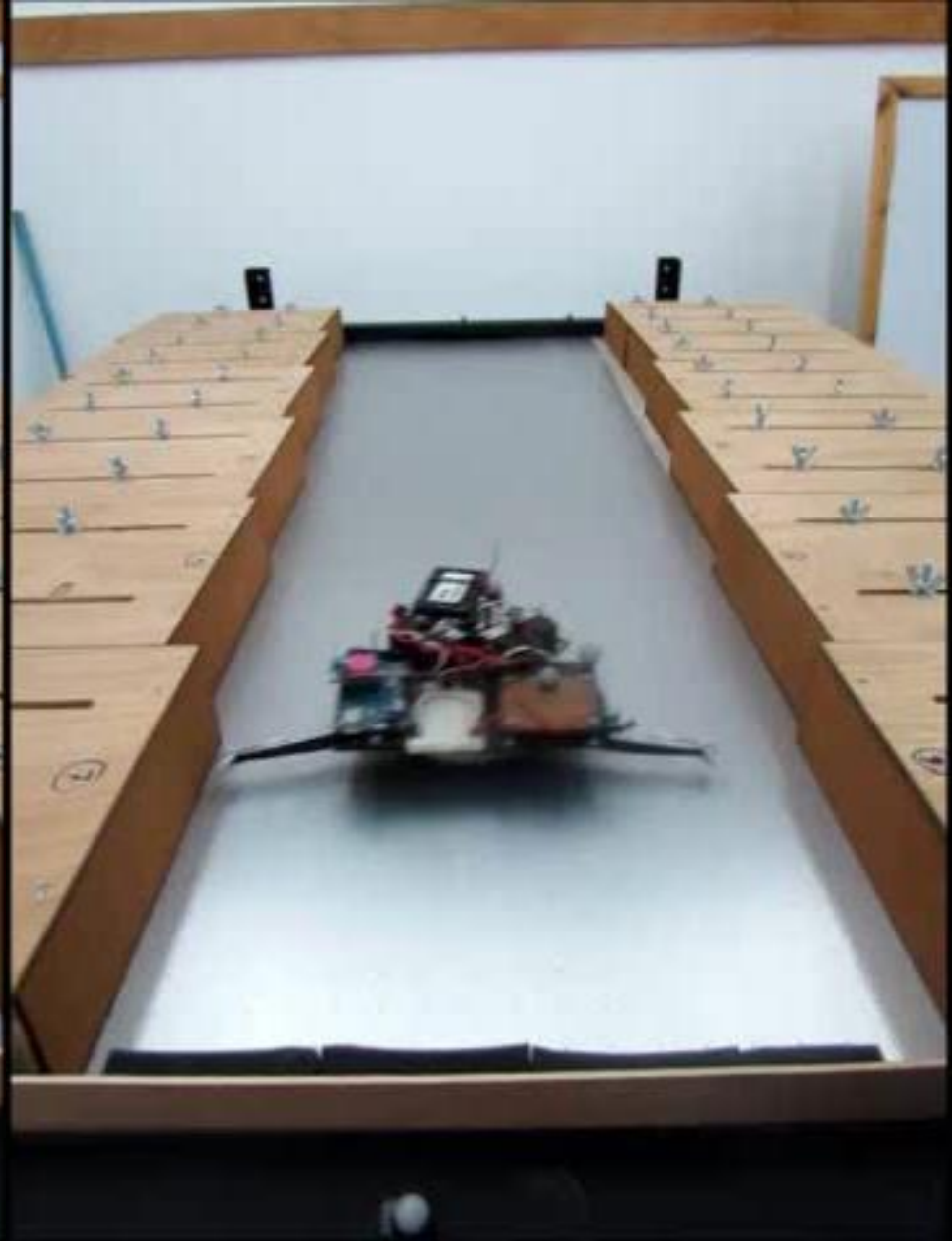
Experimental Setup







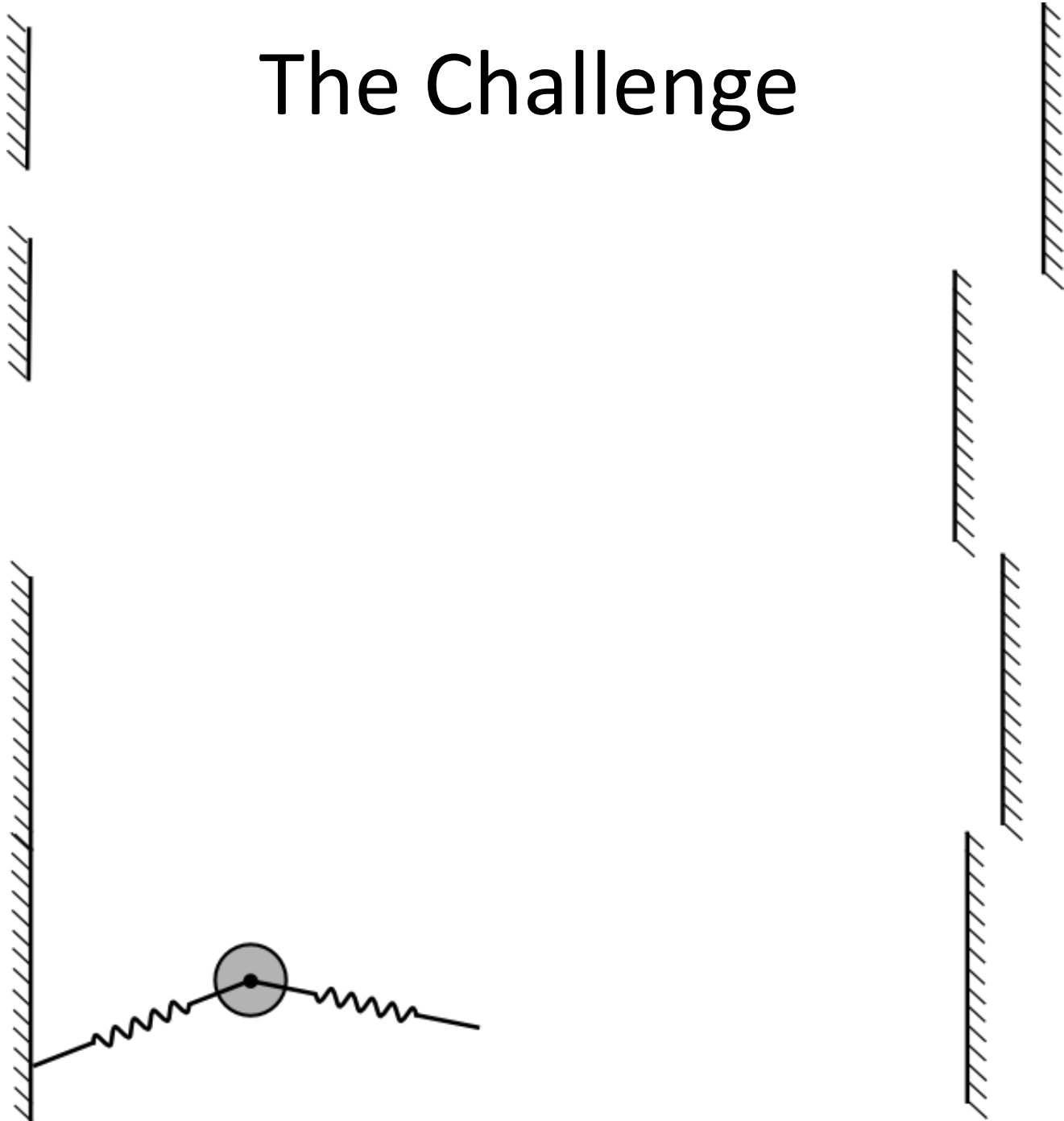
No Swing-Leg



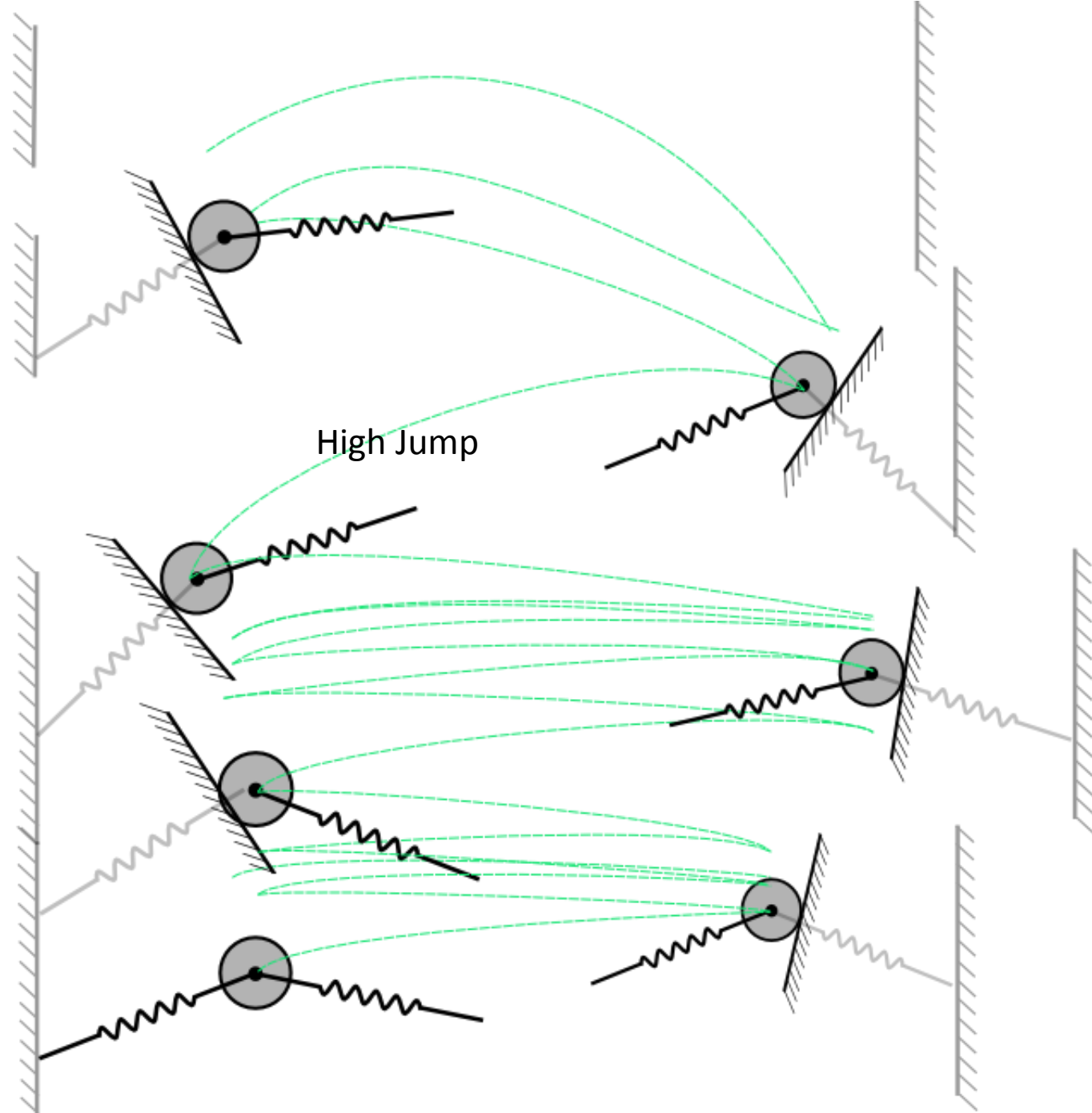
Swing-Leg

Motion Planning and Control

The Challenge







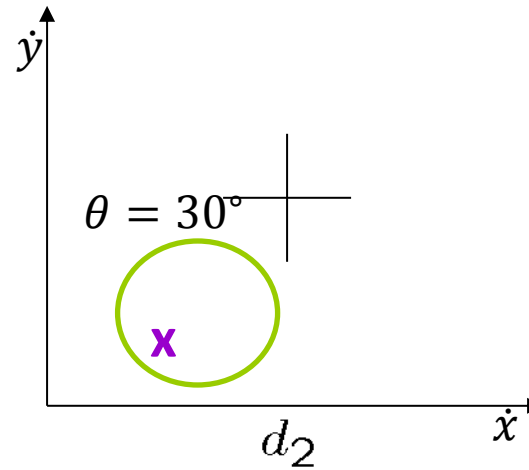
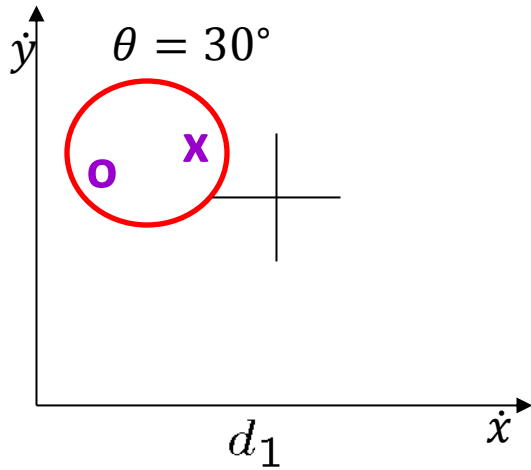
Long Jump

Increase Velocity

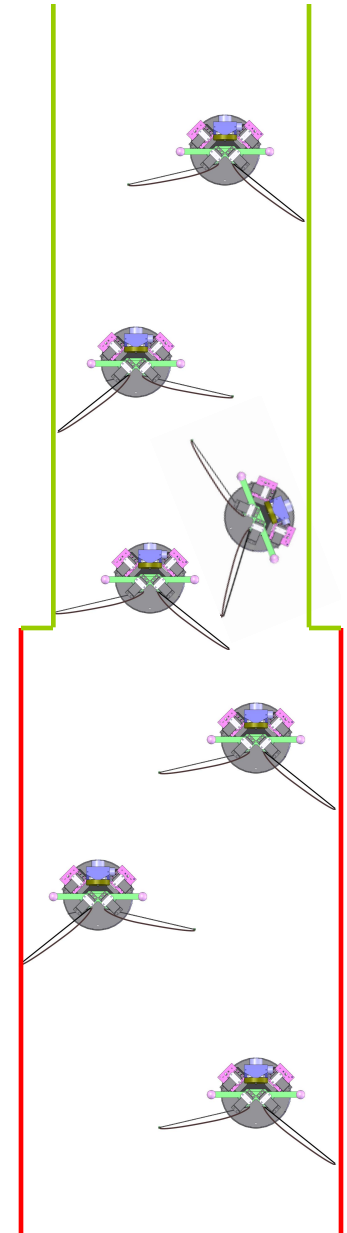
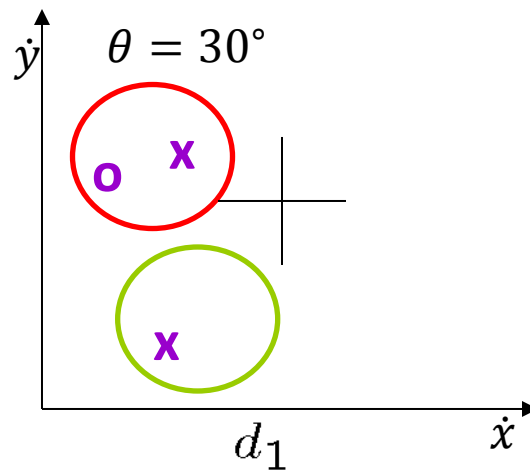
High Jump

Closed-loop

Chaining passive basins of attractions

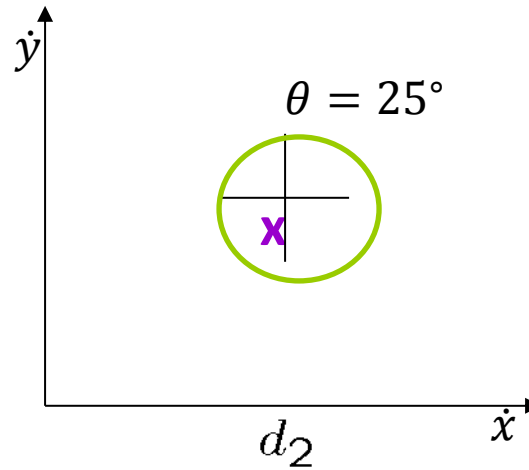
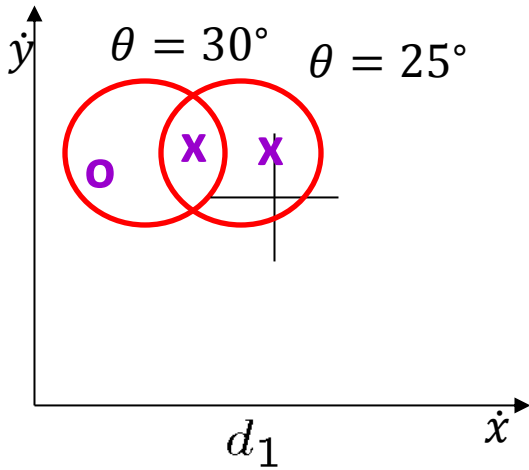


O – init. cond
X - attractor

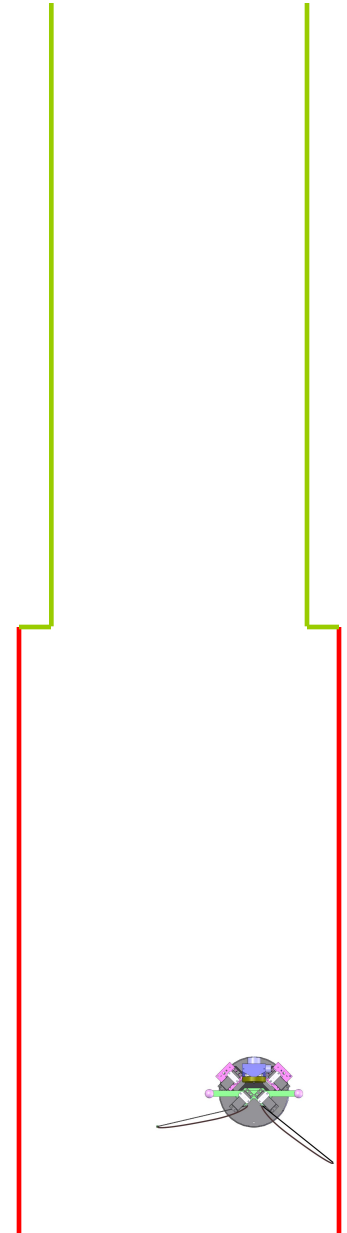
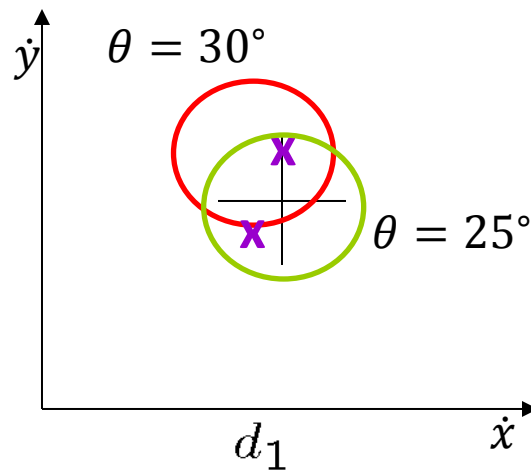


Closed-loop

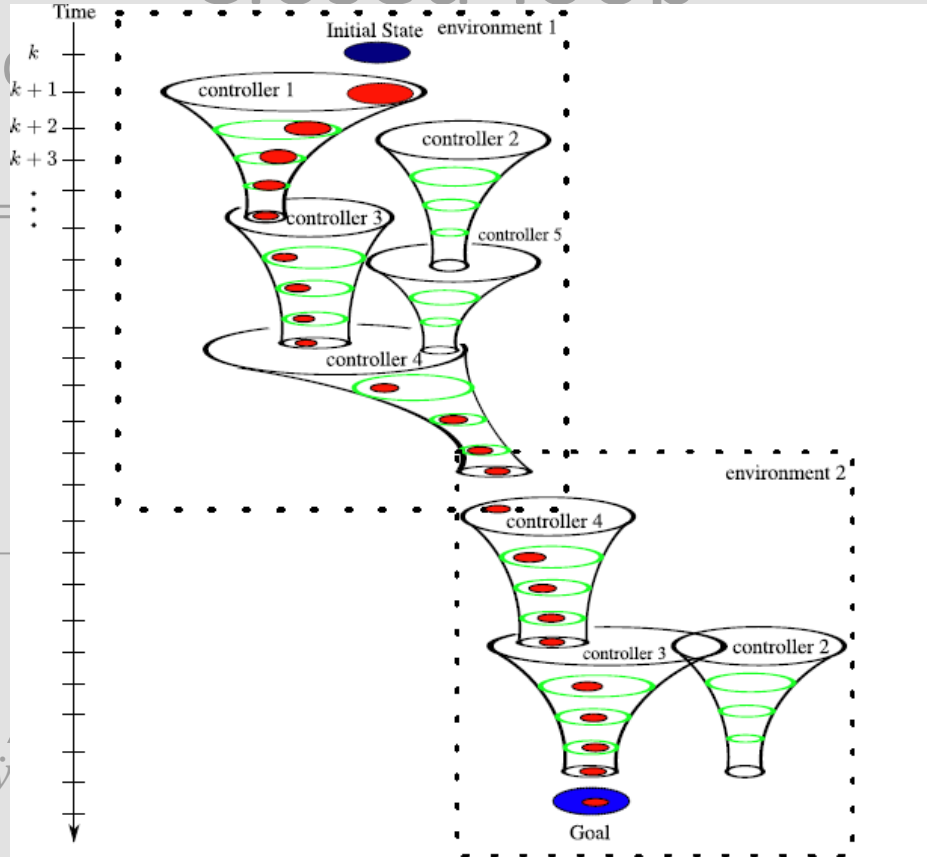
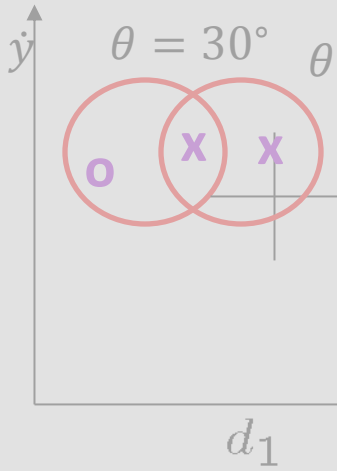
Chaining passive basins of attractions



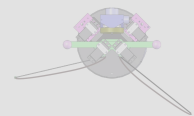
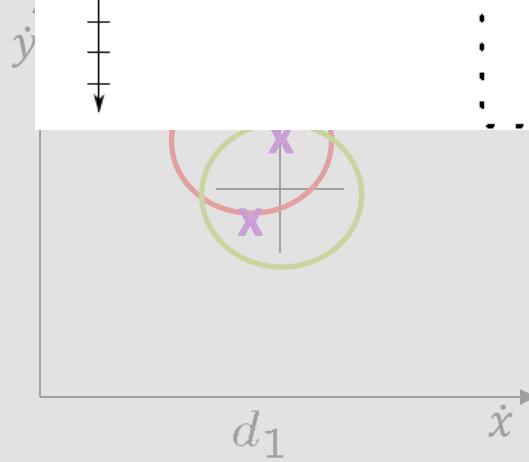
O - init. cond
X - attractor



Closed-loop

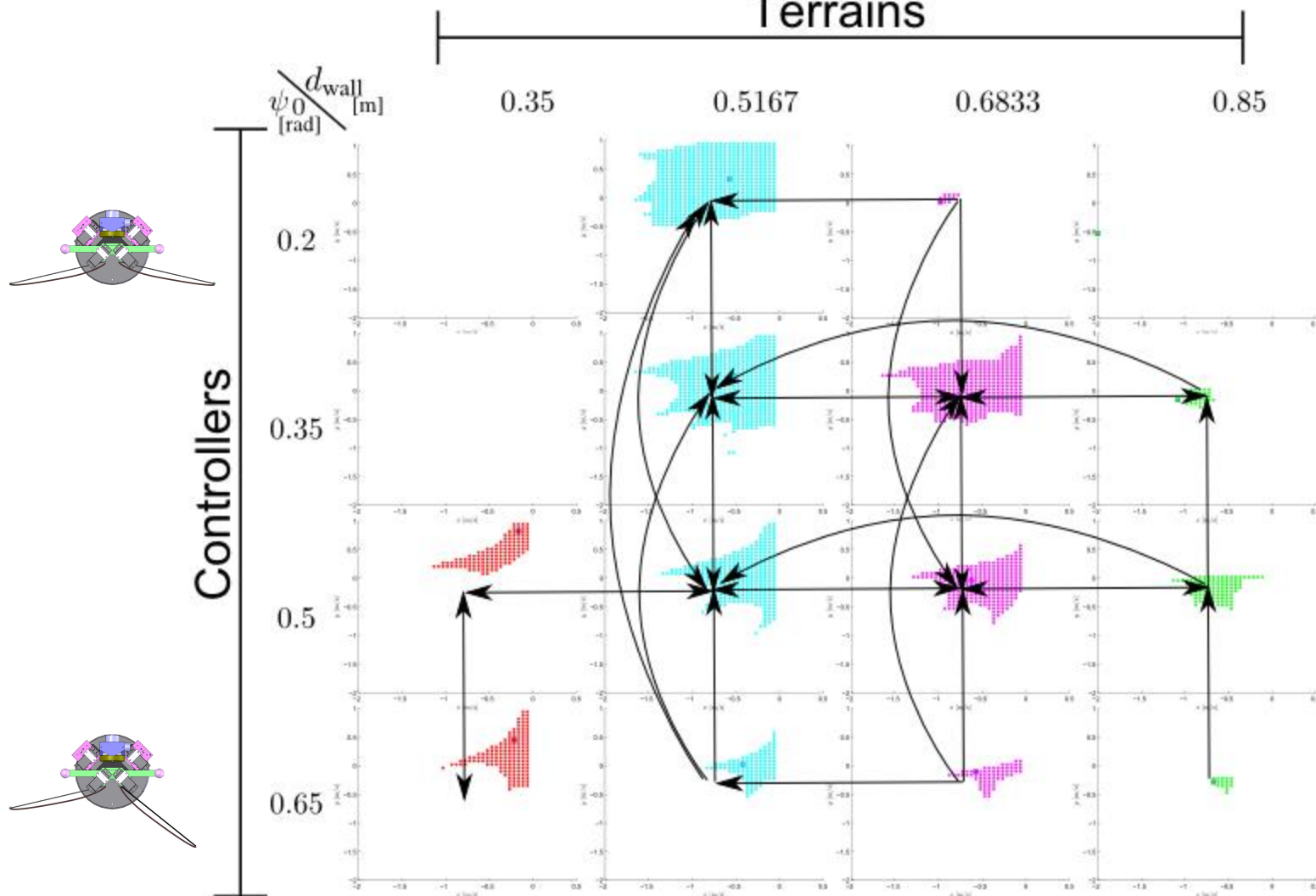


O – init. cond
X - attractor



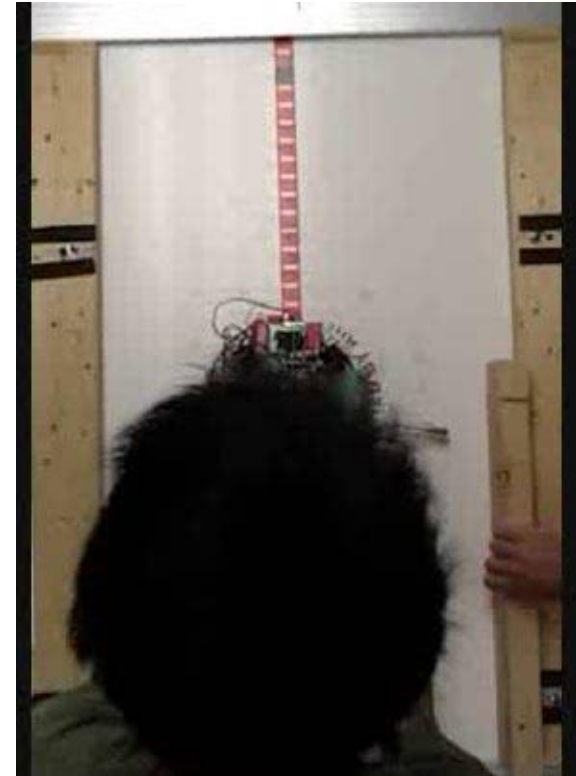
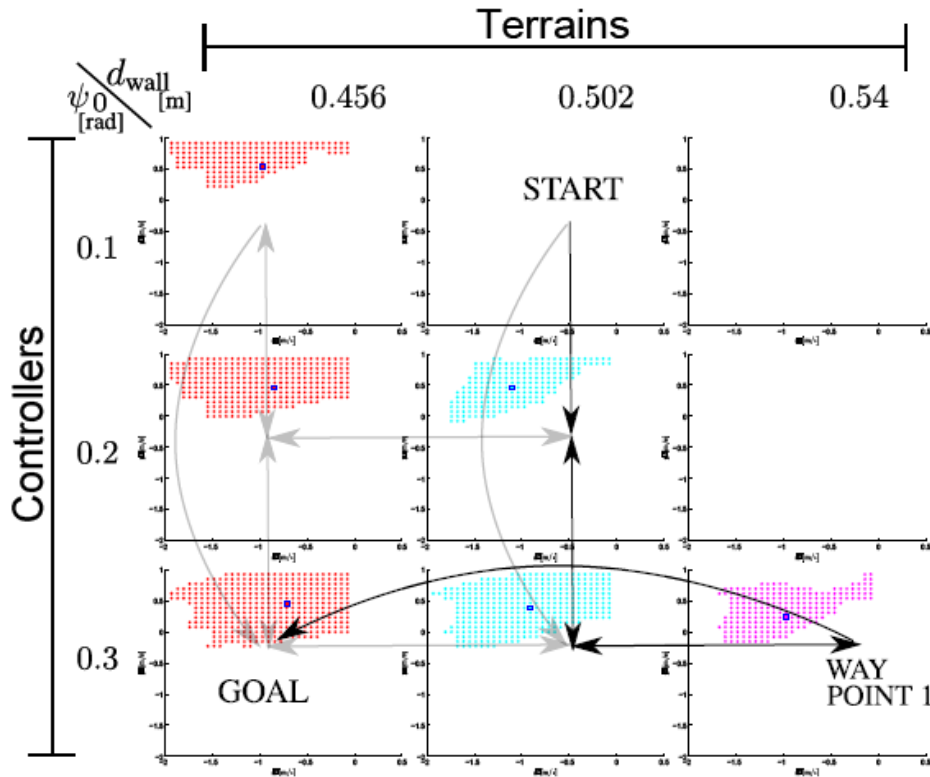
Closed-loop

Chaining passive basins of attractions

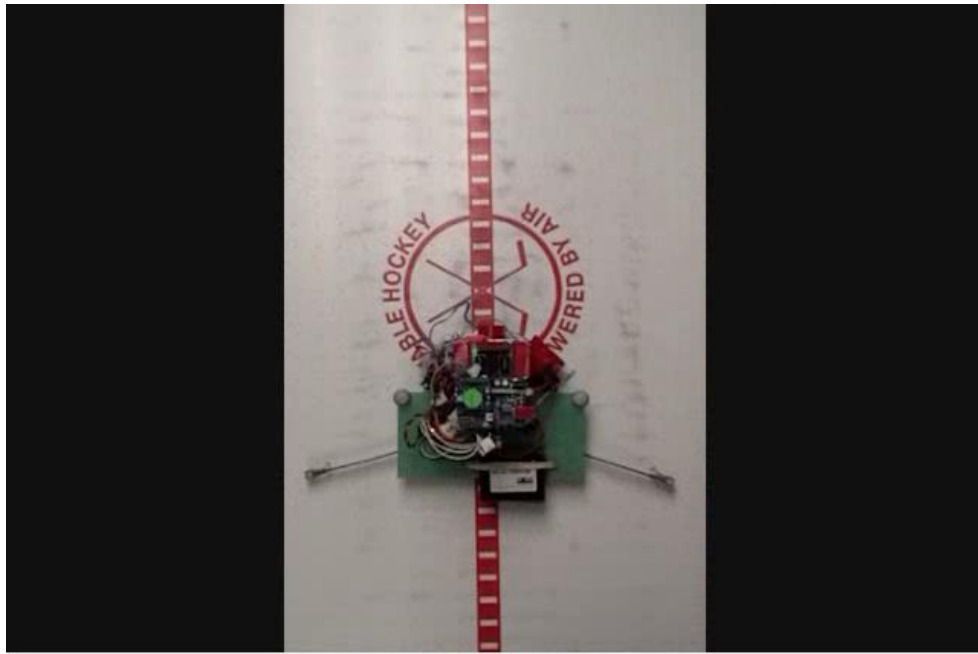
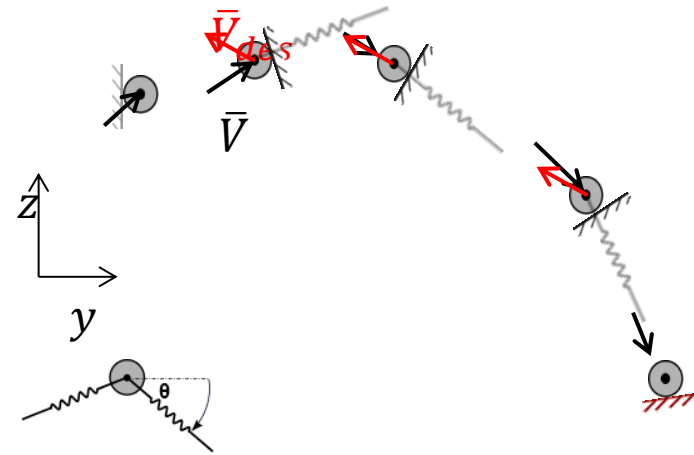
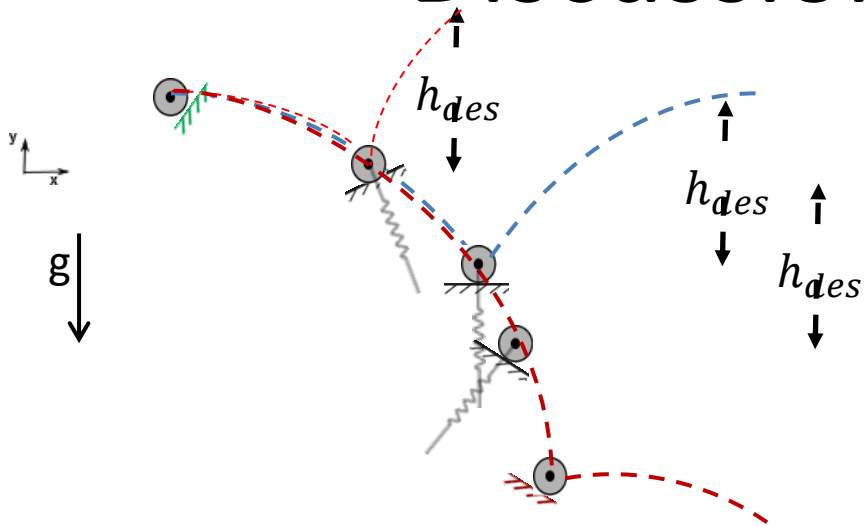


Closed-loop

Chaining passive basins of attractions



Discussion - Questions



Mechanism Design

